# Conformational effects on isobaric and constant volume specific heats in polymers

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An equation was derived for the isobaric specific heat change  $\Delta C_p$  at  $T_g$  for polymers by use of the configurational partition function normalized per unit volume for the polymer liquid. Eliminating the contributions of the conformational and free volume specific heat changes, the remaining contribution to  $\Delta C_p$ , relating to the thermal wave-length and the excess specific heat change, was considered thermodynamically. In order to investigate the causes of the abrupt change in  $C_p$  at  $T_g$  as observed in many polymers, for PE, PET, nylon-6 and PP, the conformational specific heat  $C^c$  was calculated in the temperature range from 50 K to melting temperature. The characteristic temperature dependence of  $C^c$  with a peak temperature of 100 K for PE, PET and nylon-6, 250 K near  $T_g$  (263 K) for i-PP and about 320 K for s-PP was obtained. At  $T_g$  of PE, PET and nylon-6, no peculiar change in  $C^c$  was found. The abrupt change in  $C_p$  at  $T_g$  may be attributed almost entirely to the change in the free volume specific heat  $C^f$ .

## INTRODUCTION

The isobaric specific heat change  $\Delta C_p$  at  $T_g$  for polymers, that is, the difference between the isobaric specific heats of the frozen solid and the fluid at a given temperature in the vicinity of  $T_g$ , have been considered to consist of the three components, (1) the conformational specific heat change  $\Delta C^c$ , (2) the free volume specific heat change  $\Delta C^f$ , and (3) the miscellaneous specific heat change  $\Delta C^m$ , related to the various additional modes of energy input which are required to raise the temperature of the liquid<sup>1</sup>. Roe and Tonelli have also reported<sup>1</sup> that the conformation contribution  $\Delta C^c$  to  $\Delta C_p$  is very small, the free volume contribution  $\Delta C^f$  is roughly a third to a half of the total magnitude of  $\Delta C_p$ , and the miscellaneous contribution  $\Delta C^m$  is as large as  $\Delta C^f$ .

In this paper, an equation for the isobaric specific heat change  $\Delta C_p$  at  $T_g$  will be derived by use of the configurational partition function<sup>2</sup> normalized per unit volume, taking into account both the conformational character and the free volume of the polymer liquid. Eliminating the contributions of the conformational and free volume specific heat changes, the remainder contribution, relating to the thermal wavelength and the excess specific heat change will be considered thermodynamically. The correctness of the equation for the remainder contribution will be discussed on the basis of the Roe and Tonelli's data<sup>1</sup> of the constant volume specific heat change  $\Delta C_{\nu}$  for several polymers. In the next place, in order to investigate the causes of the abrupt change in  $C_p$  at  $T_g$  as observed in many polymers, for polyethylene (PE), poly(ethylene terephthalate) (PET), nylon-6, isotactic and syndiotactic polypropylene (i-PP and s-PP), the conformational specific heat  $C^c$  will be calculated in the temperature range from 50 K to melting temperature.

## THEORETICAL AND DISCUSSION

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The isobaric specific heat change  $\Delta C_p$  at  $T_g$  for the polymers can be derived by use of the configurational partition function  $\Omega$  normalized per unit volume proposed in the preceding paper<sup>2</sup>.

$$\Delta C_p = \left[ \frac{d}{dT} \left\{ RT^2 \left( \frac{d \ln \Omega}{dT} \right) \right\} \right]_p$$
$$= \left[ \frac{d}{dT} \left\{ \left( RT^2 \frac{d \ln Z(T)}{dT} \right) / x \right\} \right]_p - \left[ \frac{d}{dT} \left( RT^2 \frac{d \ln \nu_f}{dT} \right) \right]_p + \frac{dU_0}{dT} + \frac{3}{2}R$$
(1)

where Z(T) is the conformational partition function of an isolated chain at T,  $v_f$  the free volume per structural unit,  $U_0$  the intermolecular cohesive enthalpy per molar structural unit, x the degree of polymerization, and R the gas constant. The first and second terms in the right hand side of equation (1) are respectively equal to the conformational specific heat change  $\Delta C^c$  and the free volume specific heat change  $\Delta C^f$ , and the third term  $dU_0/dT$  the excess specific heat change.

The constant volume specific heat change  $\Delta C_{\nu}$  at  $T_g$  can be derived by the thermodynamic equation:

$$\Delta C_{\nu} = \Delta C_{p} - TV \Delta(\alpha^{2}/\beta)$$
<sup>(2)</sup>

where  $\alpha$  and  $\beta$  refer to the thermal expansion coefficient and

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Table 1 The numerical values of  $\Delta C_{v}$  and  $\Delta C^{c}$  for several polymers

$\Delta C_{\nu}$ cal/g K			
Polymer	from Eq.(2)1	from Eq.(3)	$\Delta C^{C}$ cal/g K <sup>1</sup>
PS	0.042	0.041-0.047	0.011-0.017
a-PMMA	0.044	0.039	0.009
i-PMMA	0.067	0.043	0.013
PVAc	0.087	0.048-0.053	0.013-0.018
PVC	0.051	0.061	0.013



Figure 1 Conformational enthalpy  $E^{c}$  vs. temperature: (A), PE; (B), PET; (C), nylon-6

isothermal compressibility, respectively.  $TV\Delta(\alpha^2/\beta)$  is equal to the free volume contribution  $\Delta C^f$  approximately<sup>1</sup>. Therefore, from equation (1)

$$\Delta C_{\nu} \approx \Delta C^{c} + \frac{dU_{0}}{dT} + \frac{3}{2}R \tag{3}$$

The term  $(dU_0/dT + 3R/2)$  in equation (3) may be related to the miscellaneous contribution to  $\Delta C_p$  described in Roe and Tonelli's article<sup>1</sup>. The numerical values of  $\Delta C_v$  for polystyrene (PS), polymethylmethacrylate (PMMA), poly(vinyl acetate) (PVA<sub>c</sub>) and poly(vinyl chloride) (PVC), calculated from equation (2) and from equation (3) under the approximation of  $dU_0/dT \approx 0$ , are listed in Table 1, together with the numerical values of  $\Delta C^{c-1}$ .

As seen in *Table 1*, the values of  $\Delta C_{\nu}$  from equation (2) are in good agreement with those from equation (3). This result indicates that the constant volume specific heat change  $\Delta C_{\nu}$  at  $T_g$  can be evaluated theoretically by use of equation (3) and the calculated values of  $\Delta C^c$ .

## Conformation contribution C<sup>c</sup> to C<sub>p</sub>

Figures 1 and 2 show respectively the conformational



Figure 2 Conformational specific heat  $C^{C}$  vs. temperature: (A) PE (B), PET; (C), nylon-6



*Figure 3* Conformational enthalpy *E<sup>C</sup> vs.* temperature: (A), i-PP; (B), s-PP



Figure 4 Conformational specific heat  $C^{C}$  vs. temperature: (A), i-PP; (B), s-PP

enthalpy\*  $E^c$  vs. T and the  $C^c$  (=  $dE^c/dT$ ) vs. T curves for PE, PET and nylon-6. The values of  $C^c$  were obtained by the graphical differentiation method of the  $E^c$  vs. T curves in Figure 1. As seen in Figure 2, for these polymers the common peak temperature of 100 K was obtained. These peaks may be related to the motions of ethylene units contained in these polymer chains. At  $T_g$  of PE, PET and nylon-6, respectively, 153 K, 323 K and 342 K<sup>3</sup>, no characteristic change in  $C^c$  was found. Therefore, the abrupt change in  $C_p$  at  $T_g$ observed for nylon-6<sup>4</sup> and PET<sup>5</sup> may be attributed mainly to the change in  $C^f$ . Figures 3 and 4 show respectively the  $E^c$  vs. T and the  $C^c$  vs. T curves for i-PP and s-PP. For i-PP, the  $C^c$  vs. T curve has a peak temperature of 250 K near  $T_g$ (263 K)<sup>3</sup>. For s-PP,  $C^c$  has a similar peak at about 320 K. These changes in  $C^c$  near  $T_g$  for PP seem to have almost no influence on the discontinuous increment of  $dC_p/dT$  at

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 $T_g^{6-8}$ . The abrupt change in  $C_p$  at  $T_g$  may be mainly attributed to the change in  $C^f$  as well as PET and nylon-6.

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<sup>\*</sup> The calculation of  $E^c$  has been performed by use of a rotational isomeric model with three states<sup>9</sup> for PE, PET and nylon-6, and five states<sup>10</sup> for PP. For PE and PP, in which the dependences of x on  $E^c$  have been found, the values at  $x = \infty$  for PE and x = 200 for PP are used.